

Example 1. (Based on Hughes-Hallett, 4e, 3.3 Example 1) The amount of gas, G , in gallons, consumed by a car depends on the distance traveled, s , in miles. But, suppose we want to know how much gas is consumed each *hour*, not each mile? Well, the distance traveled, s depends on the time traveled, t , in hours. Let 0.05 gallons of gas be consumed for each mile traveled, and suppose that the car is traveling at 30 mi/hr . How fast is gas being consumed? Give units.

Example 2. Write each of the following functions as a function of z , where z is the “inside” function.

(a) $y = \sqrt{x^2 + 2x}$

(b) $y = 5(2x + 7)^8$

(c) $y = \frac{11}{x^2 + 1}$

(d) $y = -7.2e^{x^2}$

(e) $y = \frac{1}{2} \ln(3x^2 + 5)$

Example 3. Find the derivatives of the following functions. Use z for the inside function, and use the Leibniz notation for the chain rule.

(a) $y = 5(-3x^2 + 2x + 7)^{11}$.

(b) $y = \frac{7}{3} \ln(x^3 + x)$.

Example 4. Find the following derivatives

(a) $\frac{d}{dx}(3x - 7)^{11}$

(b) $\frac{d}{dx}\sqrt{1.9x - 4.3}$

(c) $\frac{d}{dx}\frac{1}{10x - 4}$

(d) $\frac{d}{dx}e^{1.03x-1}$

(e) $\frac{d}{dx}\ln(2x + e^2)$